

MIS: sažetak formula

Trigonometrijske funkcije (primjena na pravokutni trokut)

$$\sin(kuta) = \frac{\text{nasuprotna kateta}}{\text{hipotenuza}} ; \quad \cos(kuta) = \frac{\text{priležeća kateta}}{\text{hipotenuza}} ; \quad \tg(kuta) = \frac{\text{nasuprotna kateta}}{\text{priležeća kateta}}$$

Vektori

$$\vec{v} = v_x \hat{i} + v_y \hat{j} + v_z \hat{k} ; \quad v = |\vec{v}| = \sqrt{v_x^2 + v_y^2 + v_z^2} ; \quad \hat{v} = \frac{\vec{v}}{v}$$

Sile

2. Newtonov zakon

$$\vec{F} = \frac{d\vec{p}}{dt}$$

$$\Delta m = 0 \Rightarrow \vec{F} = m \vec{a}$$

Gravitacijska sila

$$\vec{F}_g = m \vec{g}$$

$$g = |\vec{g}| \approx 9.81 \text{ ms}^{-2}$$

Težina tijela

$$\vec{G} = m \vec{g}$$

Otpor zraka

$$\vec{F}_{OZ} = -Dv \vec{v}$$

$$D = \frac{\rho C A}{2}$$

Sila opruge

$$\vec{F} = -k \vec{x}$$

Sila gušenja

$$\vec{F} = -b \vec{v}$$

Sila trenja

$$\vec{F}_{tr} = -\mu F_{\perp} \hat{v}$$

Rezultantna sila

$$\vec{F} = \sum \vec{F}_i$$

Simuliranje translacijskog gibanja pomoću Vensima

$$\vec{a} = \frac{\vec{F}}{m}$$

$$\frac{d\vec{v}}{dt} = \vec{a}$$

$$\frac{d\vec{s}}{dt} = \vec{v}$$

$$\vec{s}(0) = \boxed{} \\ \vec{v}(0) = \boxed{}$$

Analiza gibanja pomoću Excela (analogno vrijedi za sve komponente)

0) Diskretizacija vremena (Δt dovoljno mali)

$$t_i = i \cdot \Delta t ; \quad \Delta t = t_{i+1} - t_i ; \quad i = 0, 1, 2, \dots$$

1A) Poznati: $x_i = x(t_i)$

$$v_i = \frac{x_{i+1} - x_i}{\Delta t} ; \quad a_i = \frac{v_{i+1} - v_i}{\Delta t}$$

1B) Poznati: $a_i = a(t_i)$, $v_0 = v(0)$, $x_0 = x(0)$

$$v_{i+1} = a_i \cdot \Delta t + v_i ; \quad s_{i+1} = \frac{1}{2} \cdot a_i \cdot \Delta t^2 + v_i \cdot \Delta t + s_i$$

Serijski RLC strujni krug

$$I = \frac{dQ}{dt}$$

$$\frac{dI}{dt} = \frac{d^2Q}{dt^2}$$

$$L \frac{d^2Q}{dt^2} + R \frac{dQ}{dt} + \frac{Q}{C} = 0$$

$$\omega_d = \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2}$$

Linearna regresija ($y=ax+b$)

$$a = \frac{\overline{xy} - \bar{x} \cdot \bar{y}}{\overline{x^2} - \bar{x}^2}$$

$$b = \bar{y} - a \bar{x}$$

$$\sigma_a = \sqrt{\frac{1}{n} \left(\frac{\overline{y^2} - \bar{y}^2}{\overline{x^2} - \bar{x}^2} - a^2 \right)}$$

$$\sigma_b = \sigma_a \sqrt{\overline{x^2} - \bar{x}^2}$$